If so, when does interest start to accrue on the late payment fee - and what is the interest rate?

Interest is accrued from the date that the late payment fee is charged to the account, accruing interest at the applicable purchase interest rate.